## 1 Time and location

## 2 Contact

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## 3 Aim and scope of the course

- Introduction to the numerical computation of fluid flow problems
- Techniques for analyzing numerical methods for the basic equation types (precision, stability, efficiency)
- Design of solution methods (finite differences, finite volumes)
- Supervised practical realisation of algorithms in Matlab (or similar software)

# 4 Supporting material

In order to access the lecture material, including detailed lecture notes and slides as well as the problem sheets, please register with the e-learning system "ILIAS" under the following URL:

https://ilias.studium.kit.edu/goto.php?target=crs\_2771974

# 5 Prerequisites

- Basic fluid mechanics:
  - Advection vs. diffusion processes
  - Practice in manipulating the Navier-Stokes equations

#### • Basic mathematical background:

(the chapter/section data listed in the following refers to the course by M. Neher at KIT)

- Analysis
  - \* Complex numbers (HMI, § 6.2)
  - \* Taylor series (HMI, § 15)
  - \* Fourier series (HMIII, § 7)
- Linear algebra:
  - \* vectors (HMI, § 3)
  - \* matrices and determinants (HMI, § 5)
  - \* eigenvalue analysis (HMI, § 6)

- Integral calculus:
  - \* Riemann integrals (HMII, § 1-2)
  - \* numerical integration (HMII, § 3)
- Differential equations:
  - \* ODEs (HMIII, § 1-6,8)
  - \* PDEs (HMIII, § 10)
- Fundamentals of numerical mathematics:
  - Finite-precision arithmetic, rounding, basic algorithms, ...
- Basic programming skills:
  - Previous knowledge of Matlab or similar numerical/scientific software.

## 6 Exam

Written exam, duration 90 minutes, no calculator or written notes allowed. Next exam date is: February 27, 2026.

Please register before the end of the lecture period (February 20, 2026). If not possible online, this must be done by contacting the secretariate (A. Fels, angelika.fels@kit.edu).

## 7 Contents & Planning

	Lecture				Problem session		
week $\#$		topic	date		date	assignment	
44	L1	General introduction to NFM	27.10.		29.10.	_	
45	L2	Conservation laws	03.11.	T1	05.11.	E1	
46	L3	Equation types	10.11.	T2	12.11.	E2-part1	
47	L4		17.11.	Т3	19.11.	E2-part2	
48	L5	Finite difference method	24.11.	T4	26.11.	E3-part1	
49	L6		01.12.	Т5	03.12.	E3-part2	
50	L7	Finite volume method	08.12.	Т6	10.12.	E4-part1	
51	L8		15.12.	T7	17.12.	E4-part2	
2	_		05.01.	_	<del>07.01.</del>		
3	L9	Numerical stability	12.01.	Т8	14.01.	E5	
4	L10		19.01.	Т9	21.01.	"	
5	L11	Temporal integration	26.01.	T10	28.01.	E6	
6	L12		02.02.	T11	04.02.	"	
7	L13	Linear algebra	09.02.	T12	11.02.	E7	
8	L14		16.02.	T13	18.02.	"	
9	Exam: February 27, 2026						

### 8 Other resources

- MATLAB campus license: https://www.scc.kit.edu/en/products/matlab.php
- If possible, please **bring your own laptop** to the problem sessions.

## References

- [1] C. Hirsch. Numerical computation of internal and external flows. Butterworth-Heinemann, 2nd edition, 2007.
- [2] C.A.J. Fletcher. Computational techniques for fluid dynamics. Springer, 2nd edition, 1991.
- [3] R. Peyret and T.D. Taylor. Computational methods for fluid flow. Springer, 1983.
- [4] R.J. LeVeque. Finite volume methods for hyperbolic problems. Cambridge Univ. Press, 2002.
- [5] R.J. LeVeque. Finite difference methods for ordinary and partial differential equations. Society for Industrial and Applied Mathematics, 2007.
- [6] W.H. Press, S.A. Teukolsky, W.H. Vetterling, and B.P. Flannery. *Numerical recipes in Fortran* 77. Cambridge U. Press, second edition, 1986.
- [7] U.M. Ascher and C. Greif. A first course on numerical methods. SIAM, 2011.
- [8] P.K. Kundu and I.M. Cohen. Fluid mechanics. Academic Press, 2nd edition, 2002.